

# A Model of $\text{Na}^+/\text{H}^+$ Exchanger and Its Central Role in Regulation of pH and $\text{Na}^+$ in Cardiac Myocytes

Chae Young Cha,<sup>†‡</sup> Chiaki Oka,<sup>‡</sup> Yung E. Earm,<sup>§</sup> Shigeo Wakabayashi,<sup>¶</sup> and Akinori Noma<sup>†\*</sup>

<sup>†</sup>Biosimulation Project, Faculty of Bioinformatics, Ritsumeikan University, Kusatsu, Japan; <sup>‡</sup>Biosimulation Project, Graduate School of Medicine, Kyoto University, Kyoto, Japan; <sup>§</sup>Department of Physiology, Seoul National University, Seoul, Korea; and <sup>¶</sup>Department of Molecular Physiology, National Cardiovascular Center Research Institute, Osaka, Japan

**ABSTRACT** A new kinetic model of the  $\text{Na}^+/\text{H}^+$  exchanger (NHE) was developed by fitting a variety of major experimental findings, such as ion-dependencies, forward/reverse mode, and the turnover rate. The role of NHE in ion homeostasis was examined by implementing the NHE model in a minimum cell model including intracellular pH buffer,  $\text{Na}^+/\text{K}^+$  pump, background  $\text{H}^+$ , and  $\text{Na}^+$  fluxes. This minimum cell model was validated by reconstructing recovery of  $\text{pH}_i$  from acidification, accompanying transient increase in  $[\text{Na}^+]_i$  due to NHE activity. Based on this cell model, steady-state relationships among  $\text{pH}_i$ ,  $[\text{Na}^+]_i$ , and  $[\text{Ca}^{2+}]_i$  were quantitatively determined, and thereby the critical level of acidosis for cell survival was predicted. The acidification reported during partial blockade of the  $\text{Na}^+/\text{K}^+$  pump was not attributed to a dissipation of the  $\text{Na}^+$  gradient across the membrane, but to an increase in indirect  $\text{H}^+$  production. This NHE model, though not adapted to the dimeric behavioral aspects of NHE, can provide a strong clue to quantitative prediction of degree of acidification and accompanying disturbance of ion homeostasis under various pathophysiological conditions.

## INTRODUCTION

Several types of pH-related transporters are present in the sarcolemma of cardiac myocytes. Among them, the  $\text{Na}^+/\text{H}^+$  exchanger (NHE) is regarded as the main acid extruder, in that its  $\text{H}^+$  flux is much larger than that of the other acid extruder, the  $\text{Na}^+/\text{HCO}_3^-$  cotransporter (1,2). In addition, abnormal enhancement of NHE activity under acidosis potentially induces intracellular  $\text{Na}^+$  overload through  $\text{Na}^+$  influx during pumping out excess  $\text{H}^+$  (3) and eventually  $\text{Ca}^{2+}$  overload by depressing the  $\text{Na}^+/\text{Ca}^{2+}$  exchanger (NCX). For example, the enhanced NHE has been reported to play a critical role in ischemia/reperfusion injury (4,5), and slow force response (6,7). Since regulation of all intracellular  $\text{H}^+$ ,  $\text{Na}^+$ , and  $\text{Ca}^{2+}$  concentrations within a physiological range is of vital importance in maintaining the excitability, contractility, and cell volume regulation in cardiac myocytes, a dynamic NHE model is indispensable to investigate mechanisms underlying the cellular ionic homeostasis as well as its failure under pathophysiological conditions using mathematical cell models.

A variety of mathematical models of NHE has been developed. Leem et al. (1) derived an empirical polynomial equation based on their measurements of  $\text{pH}_i$ -NHE flux relationships, and this model was used for exploring effects of acidosis on contraction and membrane excitation (8,9). NHE activity has also been described with Hill equations (10) or by a simple kinetic model (11) that attributed NHE activation to binding of intracellular  $\text{H}^+$  to its modifier site. These simple models were easy to apply, but did not provide any details of the dependencies on the intra- and extracellular

concentrations of  $\text{H}^+$  and  $\text{Na}^+$ , except for  $\text{pH}_i$ . Recently, more-complicated kinetic NHE models have been proposed (12–15), but even the latest NHE model (14) did not take account of extracellular  $\text{H}^+$  or  $\text{Na}^+$  dependencies. In addition to these classical NHE schemes, model development based on the dimer configuration of NHE (16) has been attempted (17–20). However, these models are quite different from each other and it is still difficult to distinguish them experimentally. Furthermore, in cardiac myocytes no positive proof is demonstrated for the cooperative operation of monomers within the dimeric composition. Thus, there is no available NHE model with sufficient detail to predict the contribution of NHE in intact myocytes.

In this study, we developed an NHE model, which satisfactorily reconstructs the dependencies on the intra- and extracellular concentrations of  $\text{H}^+$  and  $\text{Na}^+$  reported in the systematic experiments in the Purkinje fiber (21,22), in addition to the experimental findings in the transfected cell line (15). Subsequently, we implemented the new NHE model in a simple cell model, and found that original recordings of  $\text{pH}_i$  and  $[\text{Na}^+]_i$  variations in experiments were well explained by the alteration of NHE activity. We then examined the role of NHE under pathophysiological conditions by considering the steady-state relationship between  $\text{pH}_i$  and  $[\text{Na}^+]_i$  during depression of active  $\text{Na}^+$  transport or during long-lasting acidosis.

## METHODS

### Development of the NHE model scheme

A variety of kinetic schemes, such as ping-pong (12,13), simultaneous ion-transporting (17,18), or dimer models (19,20) have been suggested for NHE. These model schemes might equally well explain experimental findings.

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\*Correspondence: noma@sk.ritsumei.ac.jp

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Because of its applicability to a wide range of experimental data, we adopted a ping-pong scheme with 1:1 stoichiometry. Consideration of the dimeric model schemes is presented in the [Supporting Material](#).

The new kinetic NHE model is composed of two distinct functional units: an ion-exchanging part ( $j_{\text{exch}}$ ) and a proton-modifier part ( $Mod$ ). The  $H^+$  efflux or  $Na^+$  influx through NHE ( $J_{\text{NHE}}$ ) is given by the equation

$$J_{\text{NHE}}(\text{mM/ms}) = N \times Mod([H^+]_i, [H^+]_o) \times j_{\text{exch}}([H^+]_i, [H^+]_o, [Na^+]_i, [Na^+]_o) / (A \text{ vol}_i), \quad (1)$$

where  $N$  is the total number of NHE molecules,  $A$  is the Avogadro number, and  $\text{vol}_i$  is the intracellular volume.

### The ion-exchanging part ( $j_{\text{exch}}$ )

A ping-pong-type model with  $1H^+:1Na^+$  stoichiometry (23) can be described with a six- or eight-state model (Fig. 1, A or B) by assuming that  $H^+$  and  $Na^+$  either can or cannot bind simultaneously to the transporter (23). In the six-state model, the steady-state turnover rate,  $j_{\text{exch}}$ , is given as

$$j_{\text{exch}} = \frac{\frac{k_1^+ \frac{[Na^+]_o}{K_{Na}^o}}{\left(1 + \frac{[Na^+]_o}{K_{Na}^o} + \frac{[H^+]_o}{K_H^o}\right)} \frac{k_2^+ \frac{[H^+]_i}{K_H^i}}{\left(1 + \frac{[Na^+]_i}{K_{Na}^i} + \frac{[H^+]_i}{K_H^i}\right)} - \frac{k_1^- \frac{[Na^+]_i}{K_{Na}^i}}{\left(1 + \frac{[Na^+]_i}{K_{Na}^i} + \frac{[H^+]_i}{K_H^i}\right)} \frac{k_2^- \frac{[H^+]_o}{K_H^o}}{\left(1 + \frac{[Na^+]_o}{K_{Na}^o} + \frac{[H^+]_o}{K_H^o}\right)}}{\frac{k_1^+ \frac{[Na^+]_o}{K_{Na}^o}}{\left(1 + \frac{[Na^+]_o}{K_{Na}^o} + \frac{[H^+]_o}{K_H^o}\right)} + \frac{k_2^+ \frac{[H^+]_i}{K_H^i}}{\left(1 + \frac{[Na^+]_i}{K_{Na}^i} + \frac{[H^+]_i}{K_H^i}\right)} + \frac{k_1^- \frac{[Na^+]_i}{K_{Na}^i}}{\left(1 + \frac{[Na^+]_i}{K_{Na}^i} + \frac{[H^+]_i}{K_H^i}\right)} + \frac{k_2^- \frac{[H^+]_o}{K_H^o}}{\left(1 + \frac{[Na^+]_o}{K_{Na}^o} + \frac{[H^+]_o}{K_H^o}\right)}}. \quad (2)$$

In the eight-state model, it is given as

$$j_{\text{exch}} = \frac{\frac{k_1^+ \frac{[Na^+]_o}{K_{Na}^o}}{\left(1 + \frac{[Na^+]_o}{K_{Na}^o}\right) \left(1 + \frac{[H^+]_o}{K_H^o}\right)} \frac{k_2^+ \frac{[H^+]_i}{K_H^i}}{\left(1 + \frac{[Na^+]_i}{K_{Na}^i}\right) \left(1 + \frac{[H^+]_i}{K_H^i}\right)} - \frac{k_1^- \frac{[Na^+]_i}{K_{Na}^i}}{\left(1 + \frac{[Na^+]_i}{K_{Na}^i}\right) \left(1 + \frac{[H^+]_i}{K_H^i}\right)} \frac{k_2^- \frac{[H^+]_o}{K_H^o}}{\left(1 + \frac{[Na^+]_o}{K_{Na}^o}\right) \left(1 + \frac{[H^+]_o}{K_H^o}\right)}}{\frac{k_1^+ \frac{[Na^+]_o}{K_{Na}^o}}{\left(1 + \frac{[Na^+]_o}{K_{Na}^o}\right) \left(1 + \frac{[H^+]_o}{K_H^o}\right)} + \frac{k_2^+ \frac{[H^+]_i}{K_H^i}}{\left(1 + \frac{[Na^+]_i}{K_{Na}^i}\right) \left(1 + \frac{[H^+]_i}{K_H^i}\right)} + \frac{k_1^- \frac{[Na^+]_i}{K_{Na}^i}}{\left(1 + \frac{[Na^+]_i}{K_{Na}^i}\right) \left(1 + \frac{[H^+]_i}{K_H^i}\right)} + \frac{k_2^- \frac{[H^+]_o}{K_H^o}}{\left(1 + \frac{[Na^+]_o}{K_{Na}^o}\right) \left(1 + \frac{[H^+]_o}{K_H^o}\right)}}. \quad (3)$$

where  $k$  values are rate constants and the  $K$  values are dissociation constants for individual ions. It is assumed that the binding and release of ions are instantaneous, and  $K$  values are not affected by binding of  $Na^+$  or  $H^+$  in the eight-state model.

### The proton-modifier part ( $Mod$ )

Distinct from the ion-exchanging mechanism, NHE has an intracellular  $H^+$ -binding step for its activation (15). Since the value of the Hill coefficient

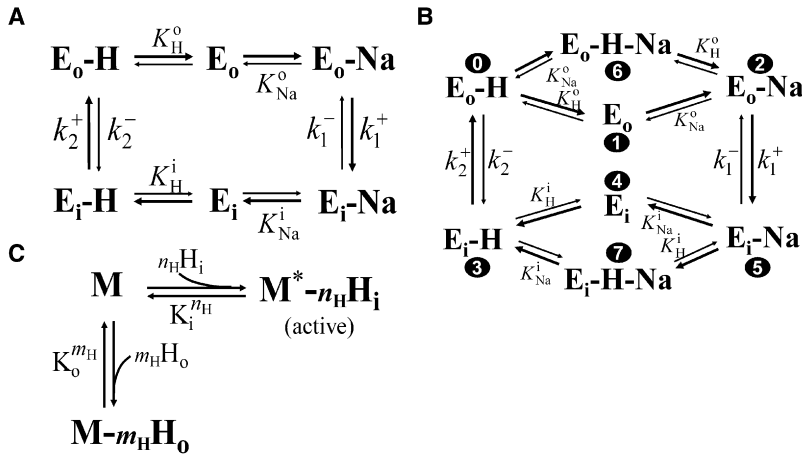
( $n_H$ ) is still a matter of debate (24,25), we tested  $n_H$  values from 1 to 4 in data fitting of a Hill equation:

$$Mod = \frac{1}{1 + \frac{(K_i)^{n_H}}{([H^+]_i)^{n_H}}}. \quad (4)$$

The  $pH_i$ - $J_{\text{NHE}}$  relationship shifted in the acidic  $pH_i$  direction with decreasing  $pH_o$  in cardiac myocytes (21,22,26) and other cell types (24,27). However, the mechanism of depression by the extracellular  $H^+$  has not been determined experimentally. Two mechanisms were considered here. First, the parallel shift may simply result from a competitive interaction between extracellular  $H^+$  and  $Na^+$  in the ion-exchanging part (24). In this case, the  $Mod$  remains the same as described by Eq. 4. Secondly, the parallel shift might occur when the extracellular  $H^+$  directly modulates the proton-modifier part (Fig. 1 C), as expressed by

$$Mod = \frac{1}{1 + \left(1 + \frac{([H^+]_o)^{m_H}}{(K_o)^{m_H}}\right) \frac{(K_i)^{n_H}}{([H^+]_i)^{n_H}}}. \quad (5)$$

$Mod$  in the former scheme is designated as  $Mod1$  (Eq. 4) and the latter as  $Mod2$  (Eq. 5). The Hill coefficient for extracellular  $H^+$  ( $m_H$ ) was



**FIGURE 1** Schemes for the NHE model. Schemes for the ion-exchanging part: the six-state model (A) and the eight-state model (B).  $E_o$  represent the state in which the binding cavity opens to the outside of the cell and  $E_i$  is the state with the binding cavity open to the inside. The thick arrows indicate the forward direction. Definitions of the parameters are given in Table S1. The numerals in panel B indicate state labels that are referred to in Fig. 9 B. (C) Schemes for the proton-modifier part (M). Ion binding was assumed to be instantaneous with equilibrium constants, the  $K$  values. The asterisk indicates the state of M that activates E.

assumed to be 1 in this study, based on the experimental finding of  $m_H = 1.2$  (21).

When the experimental data were fitted with Eq. 1,  $j_{\text{exch}}$  of a six- (Eq. 2) or eight-state (Eq. 3) model and *Mod1* (Eq. 4) or *Mod2* (Eq. 5) were examined. Since  $n_H$  ranged from 1 to 4, we examined 16 combinations of  $j_{\text{exch}}$  and *Mod* by data fitting.

### Determination of unknown parameters

The ion-exchanging part of the NHE model was expressed as a closed-loop and constrained by the following microscopic reversibility (Eq. 6), leaving nine or 10 unknown parameters to be determined (see Table S1 in the Supporting Material):

$$\frac{K_H^i K_{Na}^o}{K_H^o K_{Na}^i} = \frac{k_1^+ k_2^-}{k_1^- k_2^+}. \quad (6)$$

### Methods of fitting

The Levenberg-Marquardt fitting method was used to search for a minimum of chi-square ( $\chi^2$ ),

$$\chi^2 = \sum_{m=1}^M \left( \frac{y_m - y(x_m)}{\sigma_m} \right)^2, \quad (7)$$

where  $M$  is size of data set,  $y_m$  is experimental data of  $J_{\text{NHE}}$ ,  $y(x_m) = J_{\text{NHE}}([H^+]_i, [H^+]_o, [Na^+]_i, \text{ or } [Na^+]_o)$  defined by Eq. 1 and  $\sigma_m$  is standard deviation (SD) for the  $m^{\text{th}}$  data point. We found that the  $\chi^2$  function of  $J_{\text{NHE}}$  had numerous local minimums in 9- or 10-dimensional parameter space. Therefore, local minimums were searched with initial values which were varied systematically within a physiological range (see Table S1), and then the least  $\chi^2$  was selected among them. The interval for varying initial values should be small enough to avoid missing the global minimum of the  $\chi^2$  function. As a compromise with computational cost, 3,674,160 starting points were used in each model scheme. Further consideration of the fitting method was presented in the Supporting Material.

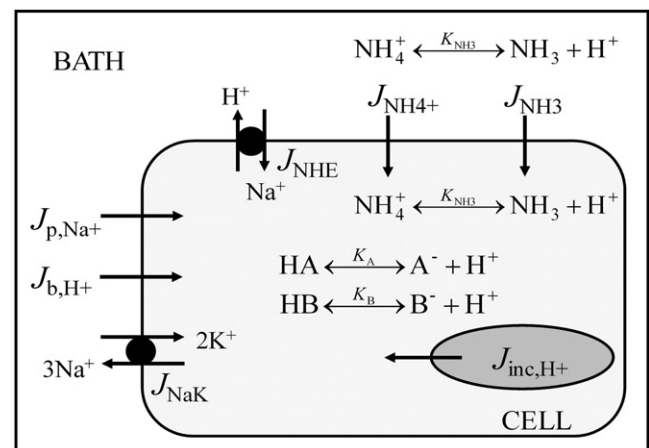
### Experimental data for determining model parameters

Selection of relevant experimental data is critical for constructing a precise model. We used three kinds of experimental data: the amplitude of  $J_{\text{NHE}}$  at various combinations of  $([H^+]_i, [H^+]_o, [Na^+]_i, \text{ or } [Na^+]_o)$ , forward/reverse mode of ionic exchange, and the NHE turnover rate.

The measurements of NHE vary due to recording techniques (ion selective electrode or fluorescent dye) or differences in specimens (species (2),

and muscles or isolated cells (28)). To minimize the experimental variations, systematic data were collected in sheep Purkinje fibers from two articles published by the same group (21,22) in which their established experimental methods were used. Alternatively, the experimental data from single ventricular myocytes might be adopted. As far as we compared, however, the configuration of  $pH_i$ ,  $pH_o$ , and  $[Na^+]_o$ - $J_{\text{NHE}}$  relationships obtained in dissociated ventricular myocyte were largely comparable to those in Purkinje fiber (see the Supporting Material). Furthermore, no measurement of  $[Na^+]_i$ - $J_{\text{NHE}}$  relationship was available in ventricular myocytes. Therefore, we considered that the use of Purkinje fiber data was appropriate.

Despite the identical experimental methods in Purkinje fibers, NHE flux was still quite variable among different preparations. To fit the data set simultaneously, the amplitude of  $J_{\text{NHE}}$  was normalized with reference to common  $pH_i$ ,  $pH_o$ ,  $[Na^+]_i$ , and  $[Na^+]_o$  in individual results. We assumed that the major subtype was NHE1 in Purkinje fibers (29) and that the diversity of NHE flux was mainly due to different sizes of tissue preparations. Finally, the data set of ion dependencies consisted of 106 data points ( $M = 106$  in Eq. 7), shown in Fig. 3 A and Fig. 4, A and B, which include a few invisible points. To calculate  $\chi^2$ , all variables in Eq. 1 and SD were



**FIGURE 2** Simple cell model of cardiac Purkinje fibers. Abbreviations:  $J_{p,Na+}$ , passive flux of  $Na^+$ ;  $J_{b,H+}$ , background  $H^+$  flux;  $J_{NHE}$ ,  $H^+$  efflux or  $Na^+$  influx through NHE;  $J_{NaK}$ ,  $Na^+$  efflux through the  $Na^+/K^+$  pump;  $J_{NH3}$  and  $J_{NH4+}$ , passive fluxes of  $NH_3$  and  $NH_4^+$ ; and  $J_{inc,H+}$ , extra flux for intracellular  $H^+$  increase by an unknown mechanism, which appears in Fig. 7.  $A^-$ ,  $B^-$ ,  $HA$ , and  $HB$ , free or  $H^+$ -bounded forms of intrinsic buffer species, A and B.

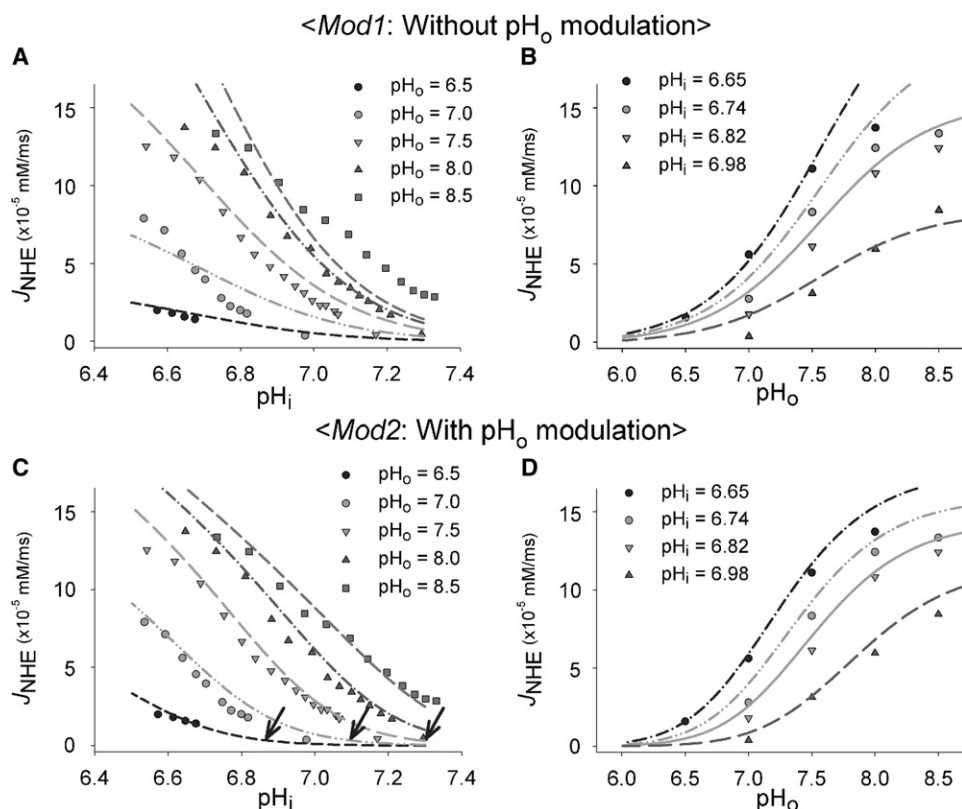


FIGURE 3 Comparison between *Mod1* and *Mod2* in response to  $pH_o$  variation. Experimental data (symbols) were taken from Vaughan-Jones and Wu (21). Various curves were plotted with the best fitting results for *Mod1* (A and B) or *Mod2* (C and D). Data points in panels B or D were selected from those in panels A or C for corresponding  $pH_i$  and  $pH_o$ , respectively. The arrows in panel C were fitted by eye to denote the location of each activation foot in the  $pH_i$ -NHE relationship at  $pH_o = 6.5, 7.0$ , and  $7.5$ , respectively. Although data points were fitted with different  $[Na^+]_i$ , an average  $[Na^+]_i$  was used to draw a continuous curve. This approximation may be justified, as the  $[Na^+]_i$ - $J_{NHE}$  relation is shallow.

required, but  $[Na^+]_i$  or SD was not always given in the literature. Therefore,  $[Na^+]_i$  was supplemented from preliminary whole-cell simulations, and the ratio between SD and the mean of  $J_{NHE}$  described in the literature (25,30) was used for obtaining SD.

The forward/reverse mode of exchange was investigated in NHE1-transfected cells by measuring  $^{22}Na^+$  flux (15). The forward mode offered information about the saturation of NHE activity at acidic  $pH_i$  below 5.2. The reverse mode provided important evidence that NHE includes a proton-

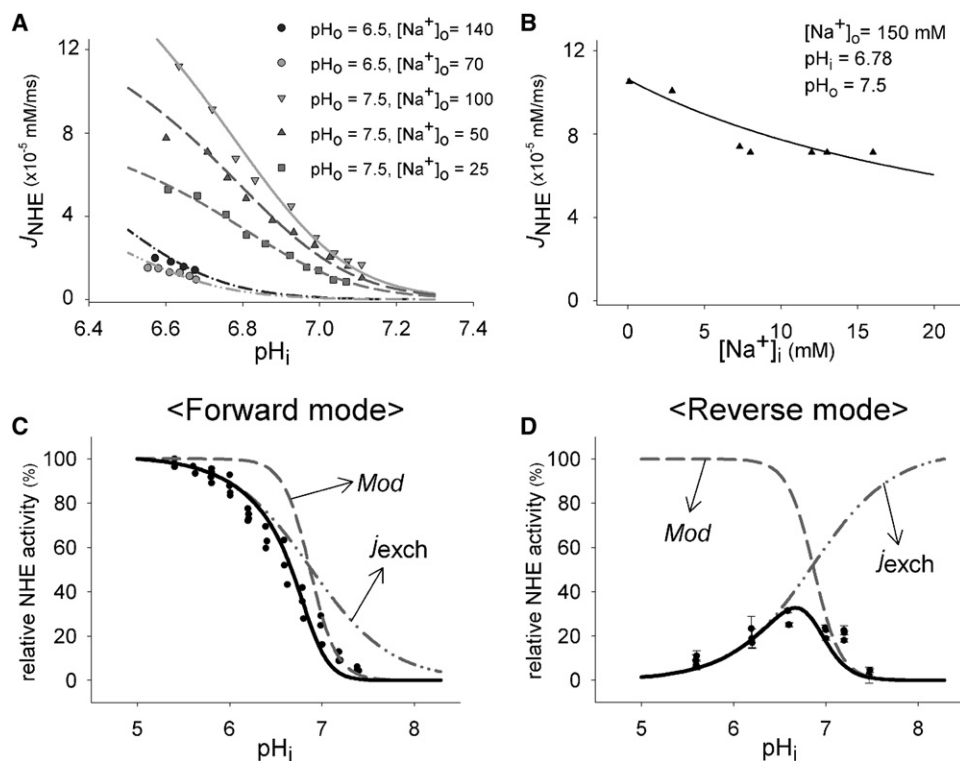


FIGURE 4 Best-fit results for NHE activity with *Mod2*. The data points in panels A and B (symbols) were taken from Wu and Vaughan-Jones (22). (A)  $pH_i$ -NHE relationship at various  $[Na^+]_o$  and  $pH_o$ . As with Fig. 3, an average  $[Na^+]_i$  was used to draw a continuous curve. (B)  $[Na^+]_i$ -NHE relationship. (C and D) The activities in the forward/reverse mode were simulated for  $[Na^+]_i/[Na^+]_o = 0/1$  or  $1/0$  mM, based on the experimental studies (15). The  $J_{NHE}$  curves (bold lines) were determined from the product of  $j_{exch}$  and *Mod* (Eq. 1).

modifier part in addition to ion-exchanging part, and helped us to determine  $j_{\text{exch}}$  and  $Mod$  separately. The turnover rate was measured by dividing  $J_{\text{NHE}}$  by total number of NHE molecules in experiments (31,32), which correspond to  $(Mod \times j_{\text{exch}})$  in Eq. 1. The turnover rate of one NHE1 molecule is  $2\text{--}10\text{ ms}^{-1}$  at  $\text{pH}_i = 6.0$ ,  $\text{pH}_o = 7.4$ ,  $[\text{Na}^+]_i \sim 0$ , and  $[\text{Na}^+]_o = 140\text{ mM}$ . We restricted this value to  $2.3\text{--}2.5\text{ ms}^{-1}$  to avoid redundancies in the fitting results due to the inverse relationship between  $N$  and  $k$  values (refer to Eqs. 1–3).

## Construction of a simple cell model

When  $\text{pH}_i$  recovers from acidification,  $[\text{Na}^+]_i$  concurrently increases due to  $\text{Na}^+$  influx through NHE. To check whether the experimental increase of  $[\text{Na}^+]_i$  during  $\text{pH}_i$  recovery is attributable to the NHE activity, we incorporated the new NHE model into a simple cell model including the minimum components involved in  $\text{pH}_i$  or  $[\text{Na}^+]_i$  regulation (Fig. 2). NBC and  $\text{Cl}^-/\text{HCO}_3^-$  exchange were not considered because they are almost inactive in a HEPES-buffered system (1). A contribution of  $\text{Cl}^-/\text{OH}^-$  exchange was included in a passive  $\text{H}^+$  flux.

The equations for individual components are presented in the Appendix. For intracellular  $\text{pH}$  buffer (Eqs. 22–25), two intrinsic buffering species, A and B, were assumed. The total concentration and dissociation constants of A and B were determined based on the measurement of intrinsic  $\text{pH}$  buffering power in Purkinje fibers (33) (see the Supporting Material). Passive  $\text{Na}^+$  flux (Eq. 13) is expressed by a constant field equation. The  $\text{pH}_i$  drift in Fig. 5 and Fig. 6 B in the absence of external  $\text{Na}^+$  might be attributed to a background  $\text{H}^+$ . This flux seems to be larger at lower  $\text{pH}_o$  or at higher  $\text{pH}_i$ , and reversed to efflux at excessive acidic  $\text{pH}_i$  (22). Although  $\text{Cl}^-/\text{OH}^-$  exchange is the potential candidate for the background  $\text{H}^+$  flux in the  $\text{CO}_2/\text{HCO}_3^-$  free conditions (34,35), other unknown mechanisms might participate. Equation 14 is used only to describe the  $\text{pH}_i$  drift of unknown nature to complete the model fitting, but is not related to biophys-

ical mechanisms. The equation for the  $\text{Na}^+/\text{K}^+$  pump (Eq. 15) was adopted from the Kyoto model (36). We described flux of  $\text{NH}_4^+$  with the constant field equation (Eq. 16) under the assumption that  $\text{NH}_4^+$  is mainly transported through inwardly rectifying  $\text{K}^+$  channels in cardiac myocytes (37). The  $\text{NH}_4^+$  flux through  $\text{Na}^+/\text{K}^+$  pump (38) or NHE (12) is neglected here, because the speed of acidification during  $\text{NH}_4\text{Cl}$  pulse is almost identical irrespective of the existence of  $\text{Na}^+$  ion in intra-/extracellular medium (Fig. 5), which might affect  $\text{NH}_4^+$  transport through  $\text{Na}^+/\text{K}^+$  pump or NHE. Flux of  $\text{NH}_3$  (Eq. 17) was expressed with Fick's law. The  $[\text{K}^+]_i$  was set to be constant, assuming that  $\text{K}^+$  permeability was dominant over others. For the same reason, the membrane potential was fixed at the  $\text{K}^+$  equilibrium potential. This approximation is justified, since changes in the flux of  $\text{Na}^+$  or  $\text{NH}_4^+$  were small when the membrane potential was altered by  $< \pm 10\text{ mV}$  around the resting potential. The extracellular ionic composition was the same as that used in the experimental studies.

## RESULTS

### Determination of the NHE model scheme and parameters

The least  $\chi^2$  for the 16 model schemes were compared for different  $n_H$  values (see Table S2). Relatively large values were obtained with  $n_H = 1$  for both *Mod1* and *Mod2*. However, it was difficult to determine which among  $n_H = 2, 3$ , and 4 was appropriate because of the marginal differences in  $\chi^2$ . For the same reason, the six- and eight-state models of  $j_{\text{exch}}$  could not be differentiated.

A more careful approach than simple comparison of  $\chi^2$  was required to discriminate *Mod1* and *Mod2* because these

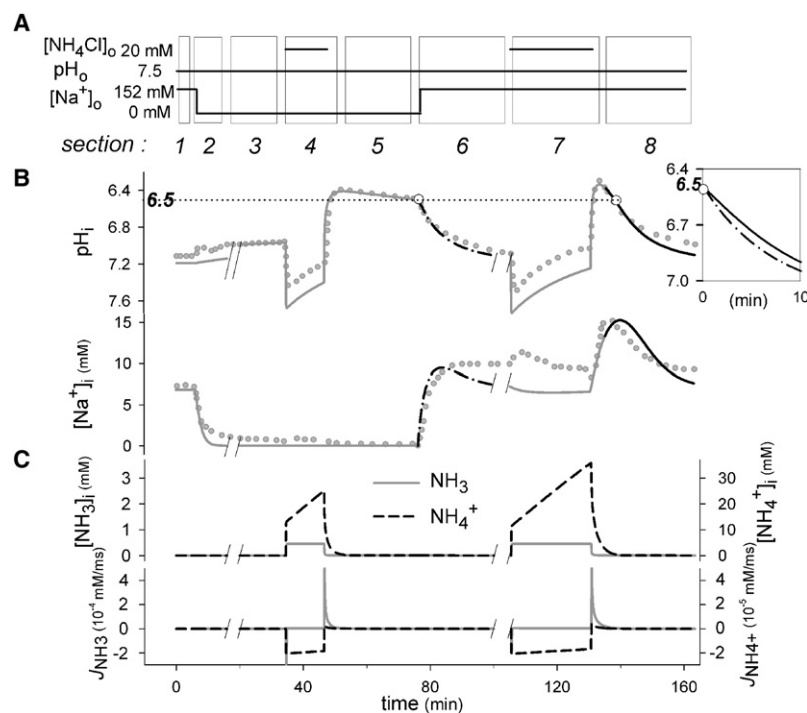


FIGURE 5 Simulation of  $\text{pH}_i$  and  $[\text{Na}^+]_i$  variations in an  $\text{NH}_4\text{Cl}$  prepulse experiment. The original experimental recordings were from Fig. 5 in Wu and Vaughan-Jones (22). (A) The experimental protocol. (B) Changes of  $\text{pH}_i$  and  $[\text{Na}^+]_i$  in the experiment (shaded dots) and in simulation (lines). (Inset) Comparison of the two recovery speeds at  $\text{pH}_i = 6.5$  between sections 6 and 8 in the simulation. Open circles indicate the time of comparison, which is indicated by a horizontal dotted line. The slash (/) denotes interruption of the simulation. (C) Simulated changes of  $[\text{NH}_3]_i$ ,  $[\text{NH}_4^+]_i$ ,  $J_{\text{NH}_3}$ , and  $J_{\text{NH}_4^+}$ . \*Simulation of the response to an  $\text{NH}_4\text{Cl}$  prepulse: The initial alkaline shift of  $\text{pH}_i$  was due to the almost instantaneous redistribution of  $\text{NH}_3$  and the following relaxation is attributable to delayed accumulation of  $\text{NH}_4^+$  within the cell. The subsequent sudden drop to  $\text{pH}_i = 6.5$  after removal of  $\text{NH}_4\text{Cl}$  was driven by the immediate and large efflux of  $\text{NH}_3$ . \*Determination of parameters for the cell model: Cellular parameters were uniquely determined from the appropriate sections.  $J_{b,H+}$  (Eq. 14) was determined from the slope of the  $\text{pH}$  change in sections 3 and 5, in which the other components were inactive due to the absence of  $\text{Na}^+$ . The amplitude of  $J_{\text{NHE}}$  ( $N$ ) was determined by the recovery rate of  $\text{pH}_i$  in sections 8, where variation of  $[\text{Na}^+]_i$  above  $8\text{ mM}$  has little effect on NHE activity (22).  $J_{\text{NaK}}$  ( $D$  in Eq. 15) and  $J_{p,\text{Na}+}$  ( $P_{\text{Na}+}$  in Eq. 13) were evaluated from the variations of  $[\text{Na}^+]_i$  in sections 1 and 2. The parameters of  $J_{\text{NH}_3}$  and  $J_{\text{NH}_4^+}$  ( $P_{\text{NH}_3}$ ,  $P_{\text{NH}_4^+}$  in Eqs. 16 and 17) were derived

from section 4.  $P_{\text{NH}_3}$  was determined by fitting the initial rising and final falling phase of  $\text{pH}_i$  record during  $\text{NH}_4\text{Cl}$  pulse, and  $P_{\text{NH}_4^+}$  from the slow acidification during the pulse and the rebound at the end of the pulse.  $P_{\text{NH}_3}$  and  $P_{\text{NH}_4^+}$  had values comparable to those in previous simulation studies (46,47), if converted with a usual surface/volume ratio (36). The acid dissociation constant of  $\text{NH}_3/\text{NH}_4^+$  ( $K_{\text{NH}_3}$ ) is  $7.08 \times 10^{-7}\text{ mM}$ . We failed to avoid the small deviation of  $\text{pH}_i$  during  $\text{NH}_4\text{Cl}$  pulse when this common  $K_{\text{NH}_3}$  was used for intracellular and extracellular medium. The values of model components are given in Table S3.



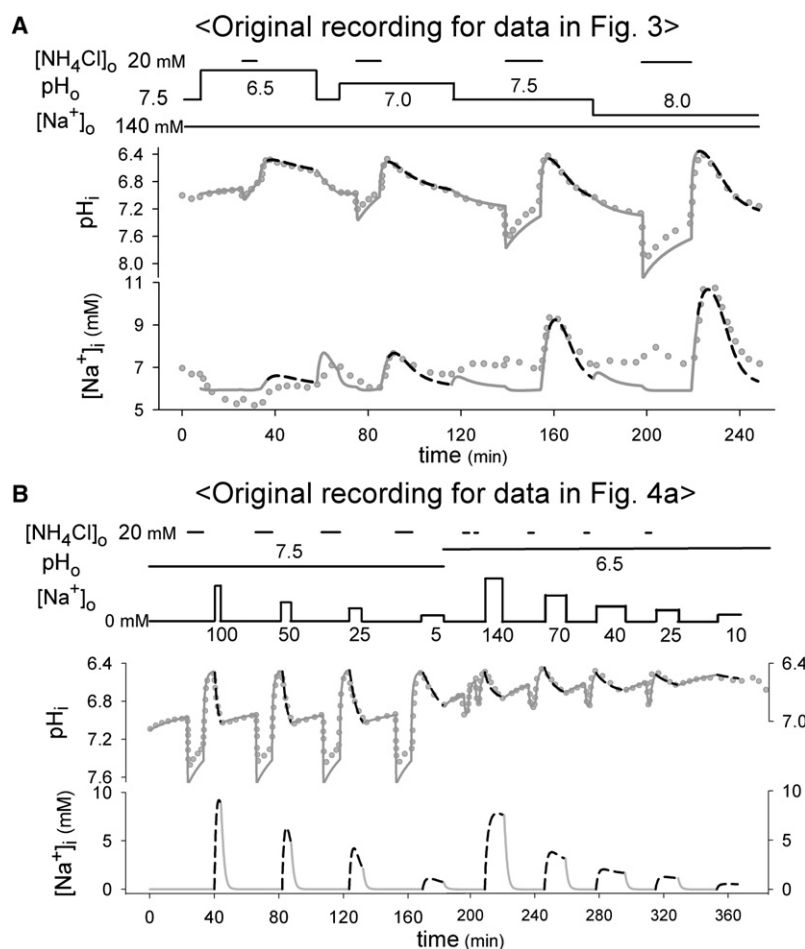


FIGURE 6 Simulations in various  $\text{pH}_o$  and  $[\text{Na}^+]_o$ . The experimental points (shaded dots) in panel A are from Fig. 6 in Vaughan-Jones and Wu (21) and those in panel B are from Fig. 1 in Wu and Vaughan-Jones (22). Dashed lines are simulated changes of  $\text{pH}_i$  and  $[\text{Na}^+]_i$  in recovery periods from acidification. The values of model parameters were determined in a similar way to that in Fig. 5, except that  $N$  was already determined in the fitting procedure. In panel B, the parameters for  $J_{\text{NaK}}$  and  $J_{\text{p,Na}^+}$  determined in Fig. 5 were used, since  $[\text{Na}^+]_i$  was not recorded in the original experiment. The values of model components are given in Table S3.

models had different numbers of unknown parameters. We found that the two models behaved differently in  $\text{pH}_o$ -induced inhibition (Fig. 3). *Mod2* could reconstruct the parallel shift of the  $\text{pH}_i$ - $J_{\text{NHE}}$  relationship; that is, the activation foot moved to lower  $\text{pH}_i$  with decreasing  $\text{pH}_o$  (arrows in Fig. 3 C). Moreover, the  $\text{pH}_o$ - $J_{\text{NHE}}$  relationship showed a clear saturation with increasing  $\text{pH}_o$  in agreement with experimental data (Fig. 3 D). In contrast, all the best-fit schemes of *Mod1* showed only scaling down in the NHE activity and failed to reconstruct the parallel shift of the  $\text{pH}_i$ - $J_{\text{NHE}}$  and saturation by  $\text{pH}_o$  (Fig. 3, A and B). Therefore, we chose *Mod2* for characterizing the modulation by  $\text{pH}_o$ , which is in accord with the extracellular allosteric regulation suggested by Vaughan-Jones and Wu (21) and Vaughan-Jones and Spitzer (39).

Among the six plausible schemes for *Mod2*, we adopted the model using  $n_H = 3$  with the eight-state ion-exchanging for the following simulations, simply because this model had the least  $\chi^2$ , regardless of whether the difference between this and the other models was significant. The final parameter set (presented in Table S1) successfully reconstructed the dependencies on  $\text{pH}_i$ ,  $[\text{Na}^+]_o$ , and  $[\text{Na}^+]_i$  (Fig. 4, A and B), as well as the forward/reverse mode of NHE (Fig. 4, C and D) (15). We found that in the forward mode, the activation

foot is determined by *Mod*, whereas the saturation at lower  $\text{pH}_i$  is dependent on  $j_{\text{exch}}$ . The slope is largely determined by cooperative activation in *Mod* with  $n_H = 3$ . In the reverse mode,  $j_{\text{exch}}$  and *Mod* change in opposite directions and  $J_{\text{NHE}}$  becomes bell-shaped.

## Reconstruction of variations of $\text{pH}_i$ and $[\text{Na}^+]_i$ in experimental recordings

### Increase in $[\text{Na}^+]_i$ in $\text{NH}_4\text{Cl}$ prepulse experiments

Wu and Vaughan-Jones (22) elaborated the experimental protocol shown in Fig. 5 A to examine effects of varying  $[\text{Na}^+]_i$  on  $J_{\text{NHE}}$ . As the cell recovered from acidification in sections 6 and 8 in simulation (as depicted in Fig. 5), the counter  $\text{Na}^+$  influx through NHE increased  $[\text{Na}^+]_i$  to levels comparable to those in the experiment (Fig. 5 B). In both experiment and simulation, the range of  $[\text{Na}^+]_i$  variation in section 6 was lower than that in section 8, and the initial rate of  $\text{pH}_i$  recovery was faster in section 6 (inset in Fig. 5). Since the simulation revealed that  $\text{NH}_3$  and  $\text{NH}_4^+$  were completely washed-out at  $\text{pH}_i = 6.5$  (Fig. 5 C), it excluded the possibility that the remaining acid loading might retard recovery (an error factor mentioned in (21)). Thus, the

simulation results support the conclusion of Wu and Vaughan-Jones (22) that the different recovery speeds were caused by the depressed NHE activity at higher  $[\text{Na}^+]_i$ . For parameters of the cell model as well as mechanisms of inducing acidification by the  $\text{NH}_4\text{Cl}$  pulse, see Fig. 5 legend.

It is essential to consider variations of  $[\text{Na}^+]_i$  as well as  $\text{pH}_i$  in evaluating the magnitude of  $J_{\text{NHE}}$ . We simulated the original recordings for obtaining the data points in Fig. 3 and Fig. 4 A, in which  $\text{pH}_o$  and  $[\text{Na}^+]_o$  were varied. In the experiment (Fig. 6 A) giving the data points in Fig. 3, the recording protocol was analogous to section 8 in Fig. 5 and  $[\text{Na}^+]_i$  varied over the range from 6 to 10 mM in both experiment and simulation. From the  $[\text{Na}^+]_i$ - $J_{\text{NHE}}$  relationship (Fig. 4 B), it is evident that the magnitude of  $J_{\text{NHE}}$  in Fig. 3 is hardly affected by variations of  $[\text{Na}^+]_i$  above 6 mM. On the other hand, the experimental protocol for the data points in Fig. 4 A (Fig. 6 B) is similar to that in section 6 in Fig. 5, and  $[\text{Na}^+]_i$  increased from virtually 0 to various peak levels during recovery from acidification. Therefore, the amplitude of  $J_{\text{NHE}}$  in Fig. 4 A was clearly modified by the  $[\text{Na}^+]_i$  variation, and that was why we supplemented individual experimental points in Fig. 4 A with corresponding values of  $[\text{Na}^+]_i$  obtained by simulations (mentioned as preliminary simulations in Methods). Taken together, these simulation results confirmed that our NHE model is applicable when extracellular conditions are changed.

#### Acidification induced indirectly by blocking the $\text{Na}^+/\text{K}^+$ pump

An increase in  $[\text{Na}^+]_i$  has been suggested to mediate the intracellular acidification when the  $\text{Na}^+/\text{K}^+$  pump is inhibited through two mechanisms:

1. A depression of NHE activity due to a decrease in the transmembrane  $\text{Na}^+$  gradient (40).
2. An induction of intracellular acidification linked to an increase of  $[\text{Ca}^{2+}]_i$  through depression of  $\text{Na}^+$ - $\text{Ca}^{2+}$  exchanger (NCX) (41,42).

First, we examined the extent of acidification induced by attenuating  $J_{\text{NHE}}$  through increased  $[\text{Na}^+]_i$  (black line in Fig. 7). When 50% of the  $\text{Na}^+/\text{K}^+$  pump was inhibited by 10  $\mu\text{M}$  strophanthidin ( $K_D = 1.12 \times 10^{-5}$  M (43)),  $[\text{Na}^+]_i$  rose rapidly toward a saturating level beyond 16 mM, in agreement with the experimental data. However,  $\text{pH}_i$  was only reduced by 0.05, which was much smaller than the experimental drop of  $\sim 0.3$ . Next, we tested the second mechanism, in which an extra  $\text{H}^+$  increment ( $j_{\text{inc,H}^+}$ ) occurs through an increase in  $[\text{Ca}^{2+}]_i$  (red line in Fig. 7) (41). If  $[\text{Ca}^{2+}]_i$  is mainly equilibrated by NCX in cardiac myocytes,  $[\text{Ca}^{2+}]_i$  is a function of  $[\text{Na}^+]_i^3$ , provided that  $[\text{Ca}^{2+}]_o$  and  $[\text{Na}^+]_o$  remain constant:

$$\frac{[\text{Ca}^{2+}]_i}{[\text{Ca}^{2+}]_o} = \left( \frac{[\text{Na}^+]_i}{[\text{Na}^+]_o} \right)^3 \exp\left(\frac{V_m F}{RT}\right) \quad (8)$$

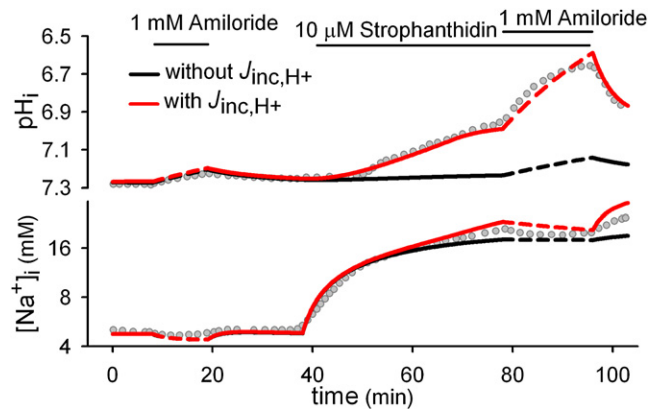


FIGURE 7 Effects of blocking the  $\text{Na}^+/\text{K}^+$  pump on  $\text{pH}_i$  and  $[\text{Na}^+]_i$ . The original experimental recordings (gray dots) are taken from Fig. 2 in Kaila and Vaughan-Jones (42). Simulation results with (red lines) or without (black lines) an extra  $\text{H}^+$  increment ( $j_{\text{inc,H}^+}$ ) are shown. Dashed lines indicate changes induced by applying amiloride. Most parameter values are the same as in Fig. 5, since the experimental conditions were comparable. The amplitudes of  $j_{\text{b,H}^+}$  and  $J_{\text{NHE}}$  were slightly modified to adjust the steady-state values of  $\text{pH}_i$  and  $[\text{Na}^+]_i$  at time zero. The values of model components are given in Table S3.

(see Blaustein and Leder (44)). For simplicity, we assumed that  $j_{\text{inc,H}^+}$  is linearly proportional to  $[\text{Ca}^{2+}]_i$  (or  $[\text{Na}^+]_i^3$ ) within a limit (Eq. 18). In consequence, a decline of  $\text{pH}_i$  with an obvious delayed onset was obtained as in the experiment (see also (40)). In addition, the simulation successfully reconstructed the increased rate of acidification and the decrease of  $[\text{Na}^+]_i$  during the complete blockage of NHE in the presence of strophanthidin in comparison to the control run. Although Eq. 18 is only a phenomenological description, the simulation supports the view that a  $\text{Ca}^{2+}$ -induced  $\text{H}^+$  increment from an unknown origin contributes to acidification to a larger extent than depression of  $J_{\text{NHE}}$  through an increase in  $[\text{Na}^+]_i$ .

## DISCUSSION

Here, for the first time to our knowledge, we have reconstructed the transient increase in  $[\text{Na}^+]_i$  accompanying NHE activation at different  $[\text{Na}^+]_o$  and  $\text{pH}_o$ . So far, there are two articles that offered simulated effects of acidosis on the developed tension with a cell model including electrical excitation,  $\text{Ca}^{2+}$  dynamics by the sarcoplasmic reticulum, contraction, and the modulation of various molecular functions at acidic  $\text{pH}_i$  (9,13). In contrast to those complicated simulations, we focused our simulations totally on the Purkinje fiber experiments, which recorded the time course of  $[\text{Na}^+]_i$  variation caused by the NHE activation. For deeper understanding of regulation of  $[\text{Na}^+]_i$  at different  $\text{pH}_i$ , we will discuss functional coupling between NHE and  $\text{Na}^+/\text{K}^+$  pump during acidosis. We then determine the extent of  $[\text{Na}^+]_i$  increase induced by acidosis using steady-state  $\text{pH}_i$ - $[\text{Na}^+]_i$  relationship, and discuss  $[\text{Na}^+]_i$ - $J_{\text{NHE}}$  relationship by taking the thermodynamic driving force into account.

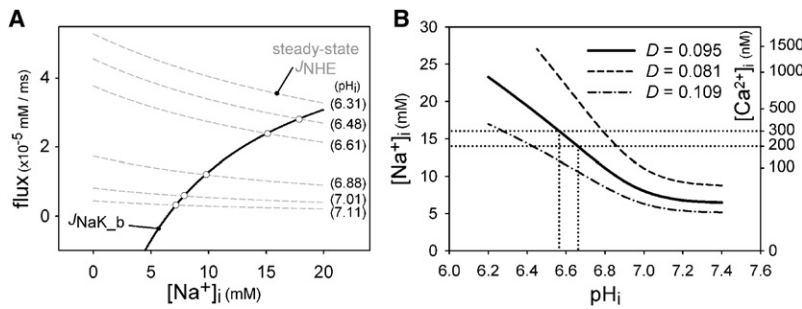


FIGURE 8 Steady-state relationship between pH<sub>i</sub> and [Na<sup>+</sup>]<sub>i</sub>. (A) Na<sup>+</sup> flux balance between  $J_{NHE}$  and  $J_{NaK\_b}$ . Gray curves indicate [Na<sup>+</sup>]<sub>i</sub>- $J_{NHE}$  at the different pH<sub>i</sub> values indicated on the right, and the black curve indicates  $J_{NaK\_b}$ . Intersections of the  $J_{NHE}$  with  $J_{NaK\_b}$  are marked with open circles. (B) The steady-state relationship between pH<sub>i</sub> and [Na<sup>+</sup>]<sub>i</sub>, corresponding to intersections of the  $J_{NHE}$  and  $J_{NaK\_b}$  in panel A. When the amplitude of the Na<sup>+</sup>/K<sup>+</sup> pump was altered from  $D = 0.095$  to  $D = 0.081$  or  $0.109$ , the curve shifted as indicated by the dashed lines. The steady-state [Na<sup>+</sup>]<sub>i</sub> on the left axis was converted to [Ca<sup>2+</sup>]<sub>i</sub> on the right axis using Eq. 8. The dotted lines indicate the critical levels of [Na<sup>+</sup>]<sub>i</sub> and pH<sub>i</sub>. The calculations were all conducted under the condition of a membrane potential of -52 mV, a reversal potential of K<sup>+</sup> at 20 mM [K<sup>+</sup>]<sub>o</sub>.

### Relationship between acidosis and [Na<sup>+</sup>]<sub>i</sub> or [Ca<sup>2+</sup>]<sub>i</sub>

The variation of [Na<sup>+</sup>]<sub>i</sub> is determined by the balance among NHE, Na<sup>+</sup>/K<sup>+</sup> pump, and passive Na<sup>+</sup> flux in our simple cell model. The time derivative of [Na<sup>+</sup>]<sub>i</sub> is

$$\frac{d[\text{Na}^+]_i}{dt} = J_{NHE} - (J_{NaK} + J_{p,Na+})$$

(see Eq. 19). Since [K<sup>+</sup>]<sub>o</sub> and the membrane potential are assumed to be constant, both  $J_{NaK}$  and  $J_{p,Na+}$  are functions of only [Na<sup>+</sup>]<sub>i</sub>. To examine the major interaction between NHE and Na<sup>+</sup>/K<sup>+</sup> pump, the sum of  $J_{NaK}$  and  $J_{p,Na+}$  is treated as  $J_{NaK\_b}$ , which is  $J_{NaK}$  biased by  $J_{p,Na+}$  (Fig. 8 A). The intersections of the  $J_{NaK\_b}$  and  $J_{NHE}$  curves correspond to  $d[\text{Na}^+]_i/dt = 0$  and give steady-state values of [Na<sup>+</sup>]<sub>i</sub> at each pH<sub>i</sub>. This steady-state relationship is demonstrated by the continuous curve in Fig. 8 B. [Na<sup>+</sup>]<sub>i</sub> is nearly constant on the alkaline side above pH<sub>i</sub> 7.2 and increases linearly with acidosis. This Na<sup>+</sup> overload during persistent acidosis may affect cellular viability via a secondary [Ca<sup>2+</sup>]<sub>i</sub> increment through NCX (45), which causes myocardial contraction. To investigate the critical level of acidosis, [Na<sup>+</sup>]<sub>i</sub> is converted to [Ca<sup>2+</sup>]<sub>i</sub> according to Eq. 8 (right axis in Fig. 8 B). Assuming that blood pumping of the ventricle is interfered with when diastolic [Ca<sup>2+</sup>]<sub>i</sub> remains higher than the activation threshold of contraction at 200 or 300 nM, the critical [Na<sup>+</sup>]<sub>i</sub> is 14–16 mM, or the critical pH<sub>i</sub> is ~6.6. The critical pH<sub>i</sub> moves in the acidic direction when  $J_{NaK}$  is

depressed, and in the alkaline direction with enhanced  $J_{NaK}$  (dotted lines in Fig. 8 B). Similarly, the change in membrane leak conductance ( $J_{p,Na+}$  in our model) under pathophysiological conditions may also affect the critical level of pH<sub>i</sub>. To get a deeper insight into the critical level of acidosis, note that the pH sensitivity of channels, transporters, and contraction should also be accounted for in the model calculation in future.

### Relationship between thermodynamic driving force and $J_{NHE}$

The variation of [Na<sup>+</sup>]<sub>i</sub> affects the  $J_{NHE}$  via thermodynamic driving force,  $E_d$ , which is given as

$$E_d = RT \times \left( \ln \frac{[\text{H}^+]_i}{[\text{H}^+]_o} + \ln \frac{[\text{Na}^+]_o}{[\text{Na}^+]_i} \right). \quad (9)$$

With a constant pH<sub>o</sub>/pH<sub>i</sub> gradient and a fixed [Na<sup>+</sup>]<sub>o</sub>,  $E_d$  is a linear function of  $\ln([\text{Na}^+]_i)$  and reverses its sign at an equilibrium value of [Na<sup>+</sup>]<sub>i</sub> (Fig. 9 A). It should be noted that our model successfully defines the equilibrium value of [Na<sup>+</sup>]<sub>i</sub> by adopting microscopic reversibility. Fig. 9 A indicates that the magnitude of  $J_{NHE}$  saturates below 3 mM [Na<sup>+</sup>]<sub>i</sub> despite the linear increase of  $E_d$ . The dependency of  $J_{NHE}$  on  $E_d$  is given by the following equation, in analogy to Ohm's law,

$$J_{NHE} = gE_d, \quad (10)$$

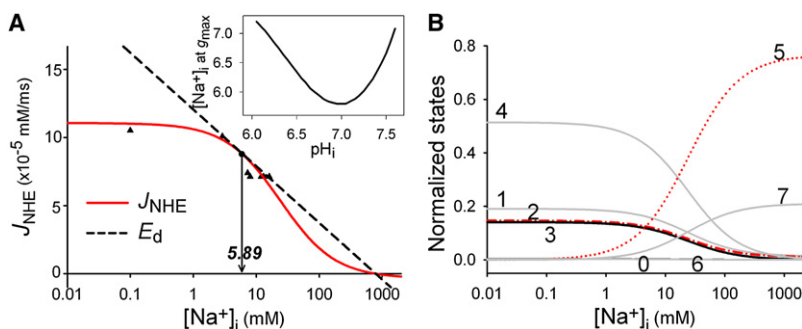


FIGURE 9 Variation of  $J_{NHE}$  and  $E_d$ , and transition of model states with [Na<sup>+</sup>]<sub>i</sub>. (A) The [Na<sup>+</sup>]<sub>i</sub>- $J_{NHE}$  relationship (solid line) and  $E_d$  (dashed line) with a log scale for [Na<sup>+</sup>]<sub>i</sub>.  $J_{NHE}$  and data points (triangles) are identical, as shown in Fig. 4 B.  $E_d$  is zero at [Na<sup>+</sup>]<sub>i</sub> = 787 mM at pH<sub>i</sub> = 6.78, pH<sub>o</sub> = 7.5, and [Na<sup>+</sup>]<sub>o</sub> = 150 mM. (Inset) Point of tangency for  $g_{max}$  at each pH<sub>i</sub>. (B) Distribution of states for the ion-exchanging part as a function of [Na<sup>+</sup>]<sub>i</sub>. Numerals indicate the states of NHE model, as defined in Fig. 1 B.



where  $g$  is the conductance of NHE ( $\text{mol J}^{-1} \text{ms}^{-1}$ ) and is defined by the slope connecting each point on the  $J_{\text{NHE}}$  curve with the equilibrium point. The maximum  $g$ ,  $g_{\text{max}}$ , appeared at  $[\text{Na}^+]_i = 5.89 \text{ mM}$ , which is defined by a tangent line to the  $J_{\text{NHE}}$  at  $\text{pH}_i = 6.78$ . The values of  $[\text{Na}^+]_i$  giving  $g_{\text{max}}$  were explored at various  $\text{pH}_i$  and are plotted against  $\text{pH}_i$  (inset of Fig. 9). It is evident that  $[\text{Na}^+]_i$  at  $g_{\text{max}}$  remains in a narrow range over a wide range of  $\text{pH}_i$ ; that is, the NHE model operates almost at  $g_{\text{max}}$  over the physiological range of  $[\text{Na}^+]_i$ , even during severe acidosis.

The  $[\text{Na}^+]_i$  dependency of  $J_{\text{NHE}}$  or  $g$  is determined by the state distributions of the ion-exchanging part of the NHE model, as shown in Fig. 9 B:

$$J_{\text{NHE}} \propto (\text{state } 2)k_1^+ - (\text{state } 5)k_1^-. \quad (11)$$

When intracellular  $\text{Na}^+$  is depleted, state 5, in which  $\text{Na}^+$  binds on the intracellular side, becomes nearly 0. Accordingly,  $J_{\text{NHE}}$  is only dependent on state 2, thereby causing  $J_{\text{NHE}}$  to saturate. As  $[\text{Na}^+]_i$  increases, states 5 and 7 accumulate at the expense of all the other states. An integrated effect of the variations of states 2 and 5 induces a gradual decay of  $g$  with increasing  $[\text{Na}^+]_i$ . Thus, the state rearrangement produces the sigmoidal dependency of  $J_{\text{NHE}}$  on  $[\text{Na}^+]_i$  (Fig. 9 A).

## APPENDIX

Equations for the simple cell model

$$CF_X = \frac{z_X F V_m}{RT} \frac{[X]_i - [X]_o \exp(-z_X F V_m / RT)}{1 - \exp(-z_X F V_m / RT)}, \text{ where} \quad (12)$$

$$X = \{\text{Na}^+, \text{NH}_4^+\}.$$

$$J_{\text{p,Na}^+} = P_{\text{Na}^+} CF_{\text{Na}^+}. \quad (13)$$

$$J_{\text{b,H}^+} = A [\text{H}^+]_o + B \text{pH}_i + C. \quad (14)$$

$$J_{\text{NaK}} = D \frac{3 \times I_{\text{NaK(in kyoto model)}}}{F \text{vol}_i}. \quad (15)$$

$$J_{\text{NH}_4^+} = P_{\text{NH}_4^+} CF_{\text{NH}_4^+}. \quad (16)$$

$$J_{\text{NH}_3} = P_{\text{NH}_3} ([\text{NH}_3]_i - [\text{NH}_3]_o). \quad (17)$$

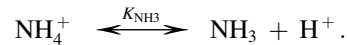
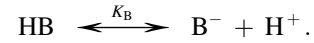
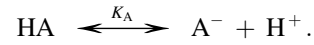
$$J_{\text{inc,H}^+} = \begin{cases} E([\text{Na}^+]_i)^3 & (\text{when } J_{\text{inc,H}^+} < \text{Max}_{\text{inc,H}^+}) \\ \text{Max}_{\text{inc,H}^+} & (\text{otherwise}) \end{cases} \quad (18)$$

$$\frac{d[\text{Na}^+]_i}{dt} = J_{\text{NHE}} - J_{\text{NaK}} - J_{\text{p,Na}^+}. \quad (19)$$

$$\frac{d([\text{NH}_3]_i + [\text{NH}_4^+]_i)}{dt} = -J_{\text{NH}_3} - J_{\text{NH}_4^+}. \quad (20)$$

$$\frac{d([\text{H}^+]_i + [\text{NH}_4^+]_i + [\text{HA}]_i + [\text{HB}]_i)}{dt} = -J_{\text{NHE}} - J_{\text{b,H}^+} - J_{\text{NH}_4^+} + J_{\text{inc,H}^+}. \quad (21)$$

The following equilibrium reactions among  $\text{NH}_3$ ,  $\text{NH}_4^+$ ,  $\text{H}^+$ , and pH buffer A and B were calculated.



$$[\text{HA}]_i + [\text{A}^-]_i = [\text{TA}]. \quad (22)$$

$$[\text{HB}]_i + [\text{B}^-]_i = [\text{TB}]. \quad (23)$$

$$K_A = \frac{[\text{A}^-]_i [\text{H}^+]_i}{[\text{HA}]_i}. \quad (24)$$

$$K_B = \frac{[\text{B}^-]_i [\text{H}^+]_i}{[\text{HB}]_i}. \quad (25)$$

$$K_{\text{NH}_3} = \frac{[\text{NH}_3]_i [\text{H}^+]_i}{[\text{NH}_4^+]_i} = \frac{[\text{NH}_3]_o [\text{H}^+]_o}{[\text{NH}_4^+]_o}. \quad (26)$$

[TA] or [TB] is the total concentration of pH buffer of A or B, respectively.  $[\text{NH}_3]_i$ ,  $[\text{NH}_4^+]_i$ , and  $[\text{H}^+]_i$  were obtained by solving Eqs. 22–26 with the iteration method.

Definitions and values of the model parameters are given in Table S3.

## SUPPORTING MATERIAL

One figure and three tables are available at [http://www.biophysj.org/biophysj/supplemental/S0006-3495\(09\)01444-1](http://www.biophysj.org/biophysj/supplemental/S0006-3495(09)01444-1).

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